A Survey of Radars Capable of Providing Small Debris Measurements for Orbit Prediction

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Introduction

- Estimates have more than 20,000 debris objects with diameters larger than 10 cm (and 600,000 with diameter larger than 1 cm) orbiting the earth (Ref: Air&Space April 6, 2011)
  - Researchers are tracking only 22,000 chunks of debris
- Debris larger than 1 cm can be lethal to current spacecraft
- The ODERACS Radar Experiments were conducted to calibrate and develop strategies for small debris detection and track\(^1\)
  - Haystack, ESA FGAN TIRA\(^2\), Russian SSN (Don-2N)\(^3\)
  - USSN (FPS-85)
- Historically, radar measurements of debris has concentrated on measuring the density of objects < 10 cm
  - US (Haystack and HAX), ESA (FGAN TIRA)
- Measurements are used to Model Debris Density and Flux to establish debris collision risk to spacecraft
- A requirement exists to track and catalog small debris
Use of Radar Sensors to Model Debris

- NASA/ESA have sponsored measurement and modeling efforts to characterize the LEO debris environment\(^4\)
  - The NASA Size Estimation Model (SEM) derives size from RCS data samples
  - NASA’s ORDEM Model and ESA’s MASTER Model are current debris models
- The US Space Surveillance Network (UHF and VHF radars) catalog builds the 1-m and 10-cm populations
  - Haystack (X-band) and HAX (Ku-band) radar data build the 1-cm population
- FGAN TIRA L-Band radar data used to validate 2-cm population

The radars do not catalog the population
Current Capability Issues

• To assess the capability of current radars to generate tracks/element sets on space debris 1 to 10 cm in diameter the issues to be addressed include:
  – The current sensitivity (detectable RCS vs range)
  – The track capability (track time, measurements errors)
    • Improvements to achieve precision small debris track data with changes in current operating modes (FPS-85 high elevation “Debris Fence”5)
• Identify multiple radar tracking network for track data exchange and experimentation

Multi Radar Network Decreases Time Between Tracks, Aids Reacquisition and Increases Cataloging Capability6,7
Radar Frequency Sensitivity

Frequencies above S-band required to detect debris down to 1 cm
World Radar Radars Able to Detect and Track Small Space Debris

- Initial 1993-1995 ODERACS experiments with calibration spheres (5, 10 and 15 cm) identified a number of radar systems that can detect small debris
  - Haystack, TIRA, Don-2N (Pill Box)
- Haystack Dish Radar was able to track the 10 and 15 cm spheres using cued search routines
- TIRA L-Band Dish Radar ODERACS measurements were statistical analyzed and compare with NASA RCS results
- Don-2N C-Band Phased Array Radar was able to detect and construct a trajectory on the 5 cm sphere using cued search routines
- FPS-85 detected and tracked <10 cm debris in special debris fence
Future Debris Radar Development

• The US is developing a Space Fence radars to provide timely assessment of space objects, events and debris
  – 2-3 geographically dispersed ground based S-Band phased array
    • Vertical Fan Beam Design, expected to detect 100,000 objects
  – First radar to be located on Kwajalein Island
    • Construction scheduled to begin in 2013 with Operational Capability planned for 2017

• ESA investing in testing space debris radar technology
  – First monostatic test radar installed in Spain in 2012
  – Second Bistatic test radar to be installed in France, worked began in September 2012
Haystack/HAX Detections

- HAX (12.2m parabolic reflector) became operational in 1994 and has been used to observe the LEO debris environment
  - Although its sensitivity is lower than Haystack it has a wider field of view (1.7 times that of Haystack)
  - The HAX observation mode is currently 75 deg east
  - The average debris diameter detected is from 2 cm to several meters (based on the NASA Size Estimation Model, SEM).
- Haystack (36.6m parabolic reflector) generally detects debris from less than 1 cm to several meters
- The Haystack/HAX debris detections are of limited quality to determine the particle’s eccentricity accurately.
  - These measurements represent statistical samplings of the population, and are thus subject to sampling error.
Haystack FY 2003 Collection
75° East

RORSAT NaK Debris is generally < 2cm
FPS-85 Detections\textsuperscript{10}

- The FPS-85 Phased Array Space Surveillance Radar, operational in 1969, is the only US phased array radar dedicated to space surveillance
  - Collects 16 million satellite observations per year
  - Can detect, track and identify up to 200 space objects simultaneously
  - Only phased array radar capable of tracking deep space objects (can track a basketball size object at 22,000nm)
    - The boresight is at 45\degree, the nominal low elevation surveillance fence is at 20\degree elevation
- The FPS-85 has upgraded software (1999) to erect a high elevation “debris” fence\textsuperscript{5}
  - Developmental testing of a fence at 35\degree enables detection of objects greater than -35dBsm
The FGAN Tracking and Imaging Radar (TIRA) is the high performance European facility able to track and image space objects.

The 34-m parabolic antenna operates with a narrow-band mono-pulse L-band tracking radar, and a high resolution Ku-band imaging radar.

The FGAN radar is sensitive enough to detect 2 cm sized objects at 1000 km.

The TIRA L-Band radar operated in beam park mode in 1994 for 24 hours in 1994 collecting debris detections.
Don-2N Detections\textsuperscript{12}

- The Don-2N (16 meter diameter) phased-array radar reached full operational capability around 1989 and was integrated into the early warning network
  - Built as a missile defense battle-management radar
  - Four face radar for 360° azimuth coverage
- The Don-2N participated in the “ODERACS” experiment in 1994\textsuperscript{13}
  - The radar was able to detect and track the smallest 5 cm sphere
  - In 2007 a launch of an ABM interceptor was made to test new computational software upgrades to the system
## Radar Parameters
(Radars in debris collection modes)

<table>
<thead>
<tr>
<th>Radar Parameter</th>
<th>FPS-85&lt;sup&gt;5,14,15&lt;/sup&gt; (Trans/Rec)</th>
<th>Haystack&lt;sup&gt;9&lt;/sup&gt;</th>
<th>HAX&lt;sup&gt;9&lt;/sup&gt;</th>
<th>TIRA&lt;sup&gt;11&lt;/sup&gt; (L/Ku)</th>
<th>Don-2N&lt;sup&gt;16&lt;/sup&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Peak Power (kW)</td>
<td>32000</td>
<td>250</td>
<td>50</td>
<td>2000/13</td>
<td>25000</td>
</tr>
<tr>
<td>Frequency (GHz)</td>
<td>0.442</td>
<td>10</td>
<td>16.7</td>
<td>1.3/16.7</td>
<td>4</td>
</tr>
<tr>
<td>Beamwidth (deg)</td>
<td>1.3/0.7</td>
<td>0.058</td>
<td>0.10</td>
<td>0.5/0.039</td>
<td>0.27</td>
</tr>
<tr>
<td>Antenna Gain (dB)</td>
<td>43/48</td>
<td>64</td>
<td>67</td>
<td>51/73</td>
<td>57</td>
</tr>
<tr>
<td>Available LFM BW (GHz)</td>
<td>0.001</td>
<td>1</td>
<td>2</td>
<td>0.06/0.8</td>
<td>0.0033</td>
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<tr>
<td>Pulse width (msec)</td>
<td>0.25</td>
<td>1.64</td>
<td>1.64</td>
<td>1/0.26</td>
<td>0.0625</td>
</tr>
<tr>
<td>Single Pulse SNR on 0dBsm @ 10&lt;sup&gt;3&lt;/sup&gt; km (dB)</td>
<td>64</td>
<td>59.2</td>
<td>40.6</td>
<td>51.2/27</td>
<td>45</td>
</tr>
</tbody>
</table>
Predicted Radar Performance\textsuperscript{17}
(Single Pulse)
Radar Measurement Errors

• The radar range measurement error, $\sigma_r$, is generally defined as the root-sum-square of three error components:

$$\sigma_r = (\sigma_{rn}^2 + \sigma_{rf}^2 + \sigma_{rb}^2)^{1/2}$$

- where $\sigma_{rn} = \Delta R/(2(S/N))^{1/2}$, $\Delta R$ is the radar range resolution approximately equal to the reciprocal of the radar bandwidth; $\sigma_{rf}$ is the range fixed random error due to random noise in the receiver and is equivalent to a 20dB S/N error; and $\sigma_{rb}$ is the range bias error, since these are the same over a series of track pulses they do not affect track results.

• The radar bandwidth, pulse width, will establish single pulse range error limits.
## Radar Measurement Errors

<table>
<thead>
<tr>
<th></th>
<th>Noise Error at Max Sensitivity (SNR 10dB)</th>
<th>Fixed Error at SNR 20dB &amp;1/50 Beamwidth</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Range Error (m)</td>
<td>Range Error (m)</td>
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<tr>
<td></td>
<td>Range Rate Error(^a) (m/s)</td>
<td>Range Rate Error(^a) (m/s)</td>
</tr>
<tr>
<td></td>
<td>Angle Error (deg)</td>
<td>Angle Error (deg)</td>
</tr>
<tr>
<td>FPS 85 LFM (max)</td>
<td>33.0</td>
<td>11.0</td>
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<tr>
<td></td>
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<td></td>
<td>0.18</td>
<td>0.026</td>
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<td>Haystack LFM (max)</td>
<td>0.03</td>
<td>0.01</td>
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<td></td>
<td>2.0</td>
<td>0.65</td>
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<td></td>
<td>0.008</td>
<td>0.0012</td>
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<td>HAX LFM (max)</td>
<td>0.02</td>
<td>0.006</td>
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<tr>
<td></td>
<td>1.3</td>
<td>0.41</td>
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<td></td>
<td>0.014</td>
<td>0.002</td>
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<tr>
<td>TIRA (L-Band) Max BW</td>
<td>0.5</td>
<td>0.07</td>
</tr>
<tr>
<td></td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>0.07</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>0.167</td>
<td>0.0014</td>
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<tr>
<td>Ron-2N Max BW</td>
<td>10.0</td>
<td>3.33</td>
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<tr>
<td></td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>0.037</td>
<td>0.0054</td>
</tr>
</tbody>
</table>

\(^a\)Assumes doppler measurement
Orbital Element Errors

• Of the six orbital elements the following three are the most accurately determined by radar measurements;
  – $i$, the inclination of the orbital plane (deg)
  – $\Omega$, the longitude of the ascending node (deg)
  – $T$, the orbital revolution period (min)
• The approximate relationships for the errors associated with these elements are given as;
  – $\sigma_\Omega = 0.0123 \left( R \sigma_\theta \pi / 180 \right) + 9.6 \left( R \sigma_r / t_r^2 \right) \sin i$ (deg)
  – $\sigma_i = 0.0123 \left( R \sigma_\theta \pi / 180 \right) + 9.6 \left( R \sigma_r / t_r^2 \right)$ (deg)
  – $\sigma_T = 48 \left( R \sigma_r / t_r^2 \right) + 0.025 \left( R \sigma_\theta \pi / 180 \right)$ (min)

where $R$ (km) is the radar range to the target, $t_r$ (sec) is the total track time, $\sigma_r$ (km) is the sigma range error, and $\sigma_\theta$ (deg) is the sigma angular error, the numerical coefficients have appropriate units to make the equations consistent
Available Fixed Beam Radar Track Time

The Fixed Beam Radars track time is based on beamwidth,
Available FPS-85 Track Time
70deg Incl, Ascending Passes thru Boresight

Array Radar track time is based on sensitivity and FOV
Cued Dish Antenna Period Error
(Single Pulse)
Phased Array Period Error
(Single Pulse)
Small Debris Cataloging
Association Criteria

- The criteria to determine track status is associated with the comparison of the estimated position of the debris object with those in the catalog,
  - Catalog correlation occurs if the object is within the association volume
  - The association volume is estimated in radial (5km), in-track (3 sec) and out of plane direction (0.05deg)
- New UCTs will be compared to previous UCTs to determine which of the UCTs correlate to develop a catalog entry
  - The criteria for UCT correlation can be 3 to 4 times that for catalog correlation (e.g., 0.2 min in-track, 0.2 deg inclination)
- Current criteria were established primarily on the basis of detecting and tracking 10 cm to 1 meter objects and the nearest neighbor distance between these objects

For the 1 to 10 cm population at the altitudes of interest association criteria needs to be assessed
Objects in a Single Pulse Search Cell

ORDEM 2000 Flux Data, 30° Lat, 45° El

Number of objects per period vs. Estimated Diameter (m)
Estimated Debris Object Separation

Poisson Probability Distribution

1000 km Altitude

Based on number in 2 orbit periods

Probability

> 1 cm

> 10 cm

Separation Distance (km)
Current Radar Capability

- TIRA, Haystack and HAX dish radars have limited small debris track time capability in a fixed beam mode
  - With cuing the HAX radar with on-pulse modulation (LFM) and track times of 20 to 30 sec accurate track data can be provided on 3 cm objects at 1000 km
  - With cuing the Haystack radar can update all small (1 to 10 cm) debris UCT element sets
    - Requires on-pulse modulation and 30 sec track times
    - Provides 0.15 min period error and 0.02 deg inclination/node error on 1 cm object at 1000 km
  - With cuing and track times to 30 sec the L-Band TIRA can provide accurate track data on 3 cm objects at 1000 km
- The Don-2N and FPS-85 phased array radars have the greatest potential to contribute uncued search and track data to a Space Debris Surveillance Network
Observations/Recommendations

• A future debris tracking radar should
  – Operate in the S-band to C-band
  – Have the sensitivity to detect/track 1 cm targets at 1800 km
  – Have agile beam capability to search and track 1 cm debris at 1800 km, track to greater 60 sec

• A small debris catalog criteria needs to be assessed
  – Assess new small object UCT criteria for period, inclination and node for the 1 to 10 cm population
  – Utilize the existing radars to gather track data in the 2 to 5 cm region and exchange data to test cataloging algorithms

• The Proposed US Air Force S-band Space Fence Concept should meet the debris tracking radar requirements and form the main element of a Space Debris Surveillance network
  – If capable the ESA test radars, Monostatic (Spain) and Bistatic (France) could provide small debris track data
  – The Don-2N and FPS-85 have the potential to contribute to a Space Debris Surveillance Network
  – TIRA, Haystack and HAX can provide future RCS measurements and updates on established element set data
References


(3) “Radar Detection and Tracking of Ballistic and Space Objects – Don-2N”, militaryphotos.net, 2004


(7) A. Nazarenko, “Model Study of the Possibilities of Space Debris Cataloging”, 9th US/Russian Space Surveillance Workshop, Siberia, Russia, August 2012

(8) D. Messier, “ESA Developing Space Safety Radar to Track Orbit Debris”, parabolicare.com/2012/09/14/esa


(10) AN/FPS-85 Phased Array Space Surveillance Radar, U.S. Air Force Fact Sheet, AFD-080219-097


(13) G. Batyr., et al., “Some Preliminary Results of the ODERACS Experiment”, proceedings of the US/Russia Orbit Determination and prediction Workshop, Washington DC, 1994


(15) J. Major, “Upgrading the Nation’s Largest Space Surveillance Radar”, Southwest Research Institute, 1994 Technology Today Article


(18) Radar System Performance Modeling – Powered by Google, Chapter 8, Radar Measurement and Tracking


All reference material is available on-line at Google Search, except the Space Surveillance Workshop Records